



THE SET OF INTEGERS ARE EQUAL TO ONE ANOTHER

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ABSTRACT: -

The integers are made up of positive numbers , negative numbers and zero .The positive numbers are the natural numbers . The integers are the real numbers .The real numbers are the rational and the irrational numbers . All integers are equal to one another .The complex numbers are made up of real numbers and imaginary numbers . The complex numbers are the sum of the imaginary numbers as well as the real numbers.

KEYWORDS: -

Positive number , Negative number, Zero, Equal , Square root

SUBJECT MATTER: -

All integers are equal to one another , So it is a paradox . Paradox is a statement, that seems to be absurd or contradictory , but it is true or it may be true .

Suppose X and Y are any two integers .

We have $(X - Y)^2 = X^2 + Y^2 - 2XY$ -----(1)

And $(Y - X)^2 = Y^2 + X^2 - 2YX$ -----(2)

Here $- 2XY = - 2YX$, As Multiplication is commutative .

From the equation (1) and the equation (2)

It is obvious that $X^2 + Y^2 - 2XY = Y^2 + X^2 - 2YX$

As $- 2XY = - 2YX$

So $(X-Y)^2 = (Y-X)^2$ -----(3)

The square root of a number x is a number

$+_y$ such that $y^2 = x$

where $-y = \sqrt{x}$ and $+y = \sqrt{x}$

The square of a negative number is positive and

the square of a positive number is also positive.

Taking the square root of both sides of the equation (3)

we get $+_- \sqrt{(X - Y)^2} = +_- \sqrt{(Y - X)^2}$

This implies that $- (X - Y) = - (Y - X)$ and

$+ (X - Y) = + (Y - X)$ ----- (4)

Taking the negative values of both sides of the equation (4)

we get $-(X - Y) = -(Y - X)$

$\Rightarrow (X - Y) = (Y - X)$ By the Left cancellation law

So $X + X = Y + Y \Rightarrow 2X = 2Y$,

So $X = Y$, By the Left cancellation law

Taking the positive values of both sides of the equation (4),

We get $X - Y = Y - X \Rightarrow X + X = Y + Y$

$\Rightarrow 2X = 2Y$

So $X = Y$ By the Left cancellation law

Hence any two integers are equal to

each other.

CASE – I All positive numbers are equal to one another

Show that $4 = 5$

Proof :- Let $X = 4$ and $Y = 5$

We have $\sqrt{(X - Y)^2} = \sqrt{(Y - X)^2}$

Putting the values of X and Y in the above equation,

We get $\sqrt{(4 - 5)^2} = \sqrt{(5 - 4)^2}$

So $4 - 5 = 5 - 4 \Rightarrow 4 + 4 = 5 + 5$

$\Rightarrow 8 = 10 \Rightarrow 2 * 4 = 2 * 5$

$\Rightarrow 4 = 5$ By Left cancellation law

Hence all positive numbers are equal to one another.

CASE – II

Any positive number is equal to zero

Show that $3 = 0$

Proof :- Let $x = 3$ and $y = 0$

we have $\sqrt{(X - Y)^2} = \sqrt{(Y - X)^2}$

Putting the values of X and Y in the above equation

We get $\sqrt{(3 - 0)^2} = \sqrt{(0 - 3)^2}$

$\Rightarrow 3 - 0 = 0 - 3 \Rightarrow 3 + 3 = 0 + 0$

$\Rightarrow 6 = 0, \Rightarrow 2 * 3 = 2 * 0$

$\Rightarrow 3 = 0$ By Left cancellation law

Hence any positive number is equal to zero

CASE – III Any positive number and any negative number are equal to each other

Show that $2 = -5$

Proof :- We have $\sqrt{(X - Y)^2} = \sqrt{(Y - X)^2}$

Let $x = 2$ and $y = -5$

Putting the values of X and Y in the above equation, we get

$\sqrt{(2 - (-5))^2} = \sqrt{(-5 - 2)^2}$

$2 + 5 = -5 - 2 \Rightarrow 2 + 2 = -5 - 5$

$\Rightarrow 4 = -10 \Rightarrow 2 * 2 = 2 * (-5)$

So $2 = -5$ By Left cancellation law

Hence any positive number and any negative number are equal to each other.

CASE – IV All negative numbers are equal to one another

Show that $-7 = -9$

Proof :- :-

We have $\sqrt{(X - Y)^2} = \sqrt{(Y - X)^2}$

Let $X = -7$ and $Y = -9$

Putting the values of X and Y in the above equation

We get $\sqrt{(-7 - (-9))^2} = \sqrt{(-9 - (-7))^2}$

$\Rightarrow -7 - (-9) = -9 - (-7)$

$\Rightarrow -7 + (-9) = -9 + (-7)$

$\Rightarrow -7 - 7 = -9 - 9$

$\Rightarrow 2 * (-7) = 2 * (-9)$

$\Rightarrow -7 = -9$ By Left cancellation law

Hence all negative numbers are equal to one another

CASE -- V Any negative number is equal to zero

Show that $-8 = 0$

Proof :-

We have $\sqrt{(X - Y)^2} = \sqrt{(Y - X)^2}$

Let $X = -8$ and $Y = 0$

Putting the values of X and Y in the above equation

We have $\sqrt{(X - Y)^2} = \sqrt{(Y - X)^2}$

$\Rightarrow -8 - 0 = 0 - (-8)$

$\Rightarrow -8 - 0 = 0 + 8$

$\Rightarrow -8 - 8 = 0 + 0$

$\Rightarrow 2 * (-8) = 2 * (0)$,

Hence $-8 = 0$ By Left cancellation law

Hence any negative number is equal to zero .

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CONCLUSION :-

The above cases show that all integers are equal to one another .